

EPSC644 Biomineralization

“Accommodation of the carbonate ion in hydroxyapatite”

Fleet, Liu and King (2004)



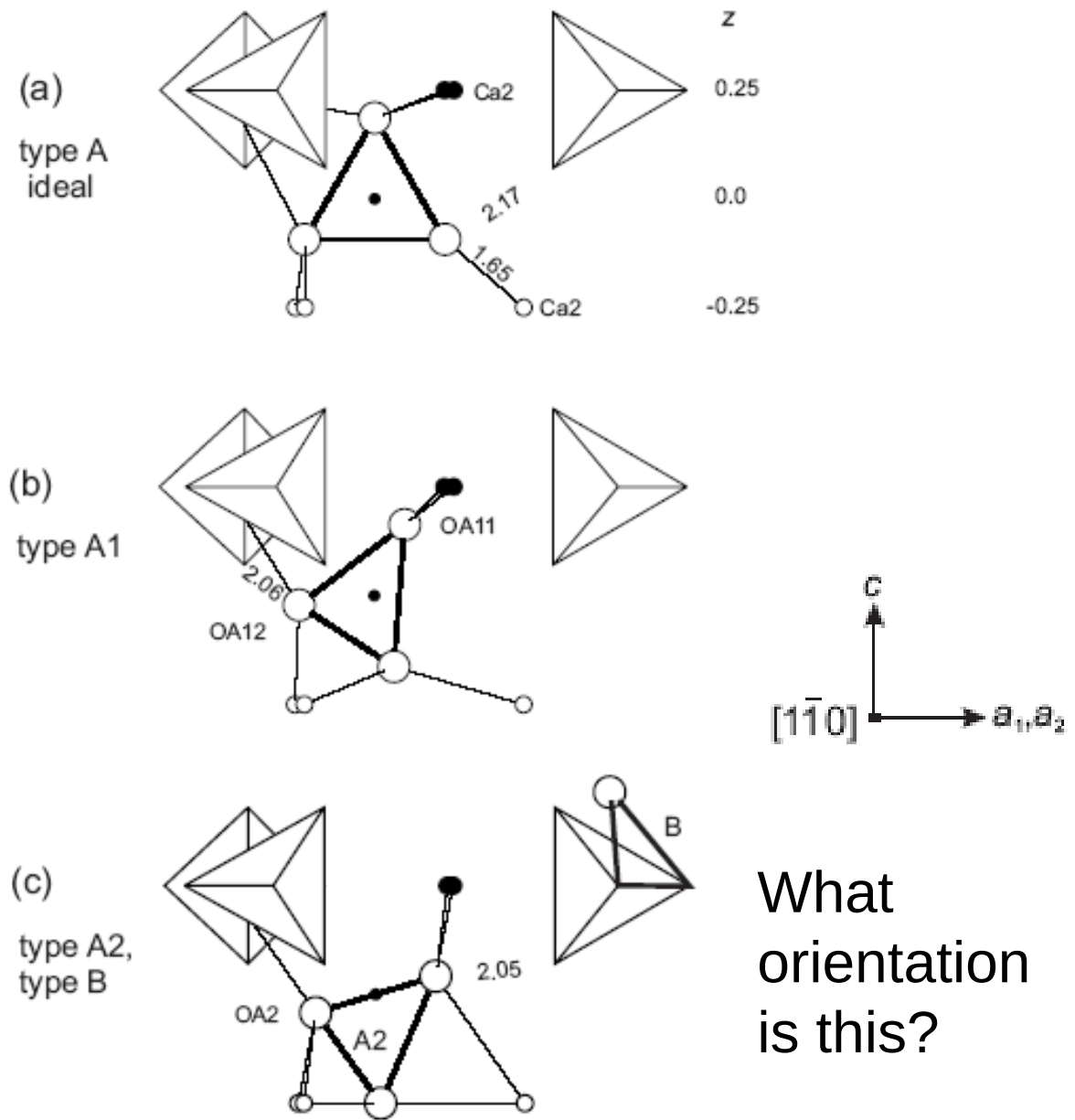
What does this equation describe?

Is anything missing from this equation?

Fig. 1

Fleet et al.  
(2004)

Caption  
mentions  
“...prohibitively  
short Ca-O and  
O-O distances  
(Å) are indicated;  
drawn with  
ATOMS (Dowty  
1995)...”  
What does this  
mean?



What  
orientation  
is this?

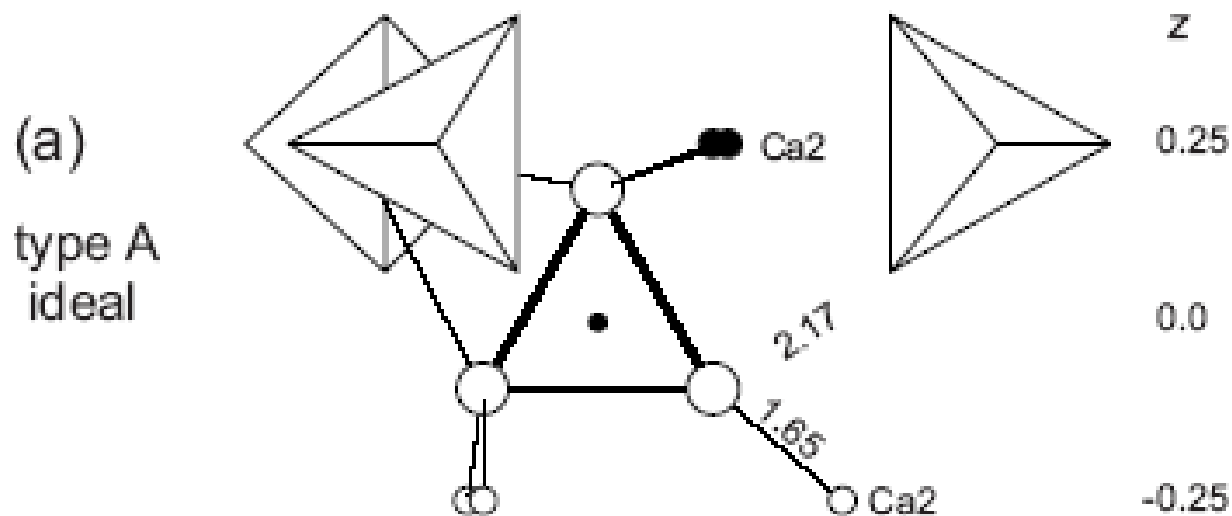
# THE SPACE PROBLEM

## Accommodation of carbonate by OHAp

The accommodation of the carbonate ion in the *c*-axis channel of hydroxylapatite is not a straightforward atom-for-atom substitution.

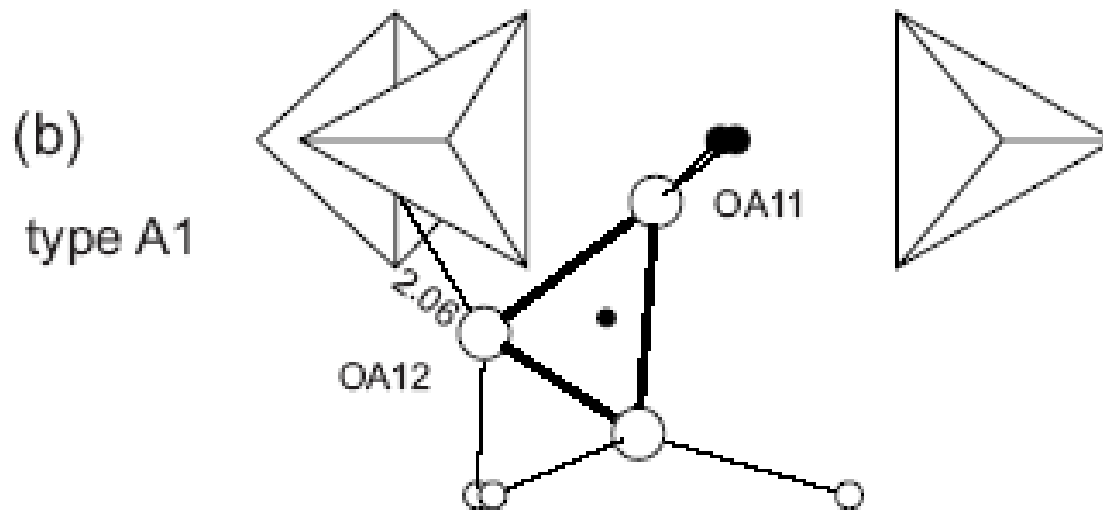
Compared with  $\text{OH}^-$ , carbonate is a bulky divalent anion (essentially a cluster of three non-bonded oxygen atoms replacing one), so that its accommodation in OHAp requires both displacement of atoms in the channel wall and redistribution of Ca-O bonds.

The type B carbonate ion is seemingly accommodated more readily, but still requires displacement of the second  $\text{O}^{3-}$  atom away from the bonding sphere of the carbonate ion and extension of the overall structure in the *c*-axis direction.

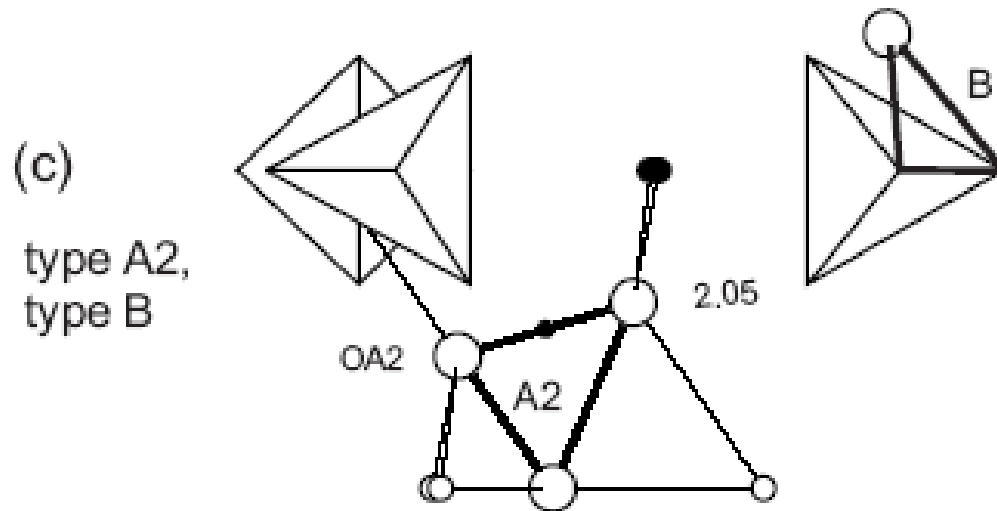


When a carbonate ion of ideal geometry is inserted into the channel of OHAp with the apical oxygen atom coincident with the position of OH, as in Figure 1a, it is evident that the other two (transverse) carbonate oxygen atoms interact unfavorably with the tricluster of Ca<sup>2+</sup> cations at  $z = -0.25$ . In the limiting orientation of Figure 1a, one of these oxygen atoms makes a short (1.65 Å) bond with a Ca<sup>2+</sup> atom and a short (2.17 Å) non-bonded O...O interaction with O3 of the nearby PO<sub>4</sub> tetrahedron.

Clearly, the carbonate ion has to be twisted about the *c*-axis to optimize Ca-O and O-O distances, but this still leaves unacceptably short interactions in the absence of other displacements.



The type A1 carbonate ion is oriented with two of its oxygen atoms (OA11) close to the c-axis and its plane canted from the vertical by  $\sim 12^\circ$ . It is located in the apatite channel by six bonds to Ca2 atoms, giving Ca2-O bond distances consistent with an ideal distribution of valence units for the carbonate ion oxygen atoms (i.e.,  $4/3$  to C and  $1/3$  to  $2 \times \text{Ca2}$ ).



This last possibility is described as a

“second (stuffed) channel position characterized by IR bands at 1563 and 1506  $\text{cm}^{-1}$ , which was present in subordinate amounts and appeared to **charge-compensate** the substitution of  $\text{PO}_4^{3-}$  by  $\text{CO}_3^{2-}$  (type A2 carbonate; Fig. 1c).”



What does this equation describe?

Is anything missing from this equation?



Maryam asked...

“Can we calculate how the morphology of hydroxylapatite would be modified by the presence of carbonate groups substituted in its structure?”

- Concept of equilibrium morphology: for every crystalline structure, there is a theoretical morphology corresponding to its lowest Gibbs free energy.

- each single crystal is bound by surfaces offering the possible lowest density of unsatisfied bonds

- this is how a crystalline solid would rearrange itself if it could freely break and reform bonds in a vacuum

- But during crystal growth from solution, the surface interacts with the solvent and its solutes.

- what is the nature of those interactions?

**TABLE 1.** Synthesis experiments

| Experiment | Starting composition* | <i>P</i> (GPa) | <i>T</i> (°C) | Time (hours) | Product†            | Reference‡ |
|------------|-----------------------|----------------|---------------|--------------|---------------------|------------|
| PC16       | 9:1                   | 4              | 1400          | 5.5          | type A C-OHAp + Cc§ | 3          |
| PC56       | 9:1                   | 3              | 1400          | 5.5          | type A CAp + Cc§    | 3          |
| PC71       | 9:1                   | 2              | 1400          | 6            | type A CAp          | 1          |
| PC74       | 9:1                   | 2              | 1500          | 12           | type A CAp          | 1          |
| PC17       | 8:2                   | 3              | 1400          | 5.5          | type B C-OHAp       | 3          |
| PC55       | 8:2                   | 3              | 1400          | 5.5          | type A-B CAp + Cc#  | 2          |
| PC73       | 8:2                   | 2              | 1450          | 6            | type A-B CAp + Cc   | 3          |
| PC18       | 7:3                   | 3              | 1400          | 5.5          | type A-B CAp + melt | 3          |
| PC53       | 7:3                   | 3              | 1400          | 5.5          |                     |            |
|            |                       |                | 1000          | 13           | type A-B CAp + Cc   | 3          |
| PC57       | 7:3                   | 3              | 1400          | 5.5          | type A-B CAp + melt | 3          |
| PC59       | 7:3                   | 3              | 1500          | 5.5          | type A-B CAp + melt | 3          |
| PC26       | 6:4                   | 2              | 1350          | 5.5          | type A-B CAp + melt | 3          |
| PC58       | 7:2:1                 | 2              | 1400          | 5.5          | type B CFAP + melt  | 3          |

\* Starting composition is proportion of  $1/3(\text{Ca}_2\text{P}_2\text{O}_7 + \text{CaO}) : \text{CaCO}_3$ ; for PC58 proportion is for  $1/3(\text{Ca}_2\text{P}_2\text{O}_7 + \text{CaO}) : \text{CaCO}_3 : \text{CaF}_2$ .

† Melt is carbonate rich.

‡ 1 is Fleet and Liu (2003); 2 is Fleet and Liu (2004); 3 is present study.

§ Trace amounts of calcite (Cc).

# PC55 products were used for annealing experiments at 1000 °C for 15 and 30 minutes, and 12 and 24 hours.

**TABLE 5.** Selected bond distances (Å)

|         |     | PC17<br>xt372 | PC16<br>xt374 | PC18<br>xt371 | PC18<br>xt373 |
|---------|-----|---------------|---------------|---------------|---------------|
| Ca1-O1  | × 3 | 2.407(1)      | 2.409(1)      | 2.420(1)      | 2.419(1)      |
| Ca1-O2a | × 3 | 2.458(1)      | 2.464(2)      | 2.479(1)      | 2.479(1)      |
| Ca1-O3a | × 3 | 2.808(2)      | 2.814(2)      | 2.809(2)      | 2.808(2)      |
| Mean    |     | 2.558         | 2.562         | 2.569         | 2.569         |
| Ca2-O1b |     | 2.708(2)      | 2.707(2)      | 2.716(2)      | 2.715(2)      |
| Ca2-O2c |     | 2.356(2)      | 2.350(2)      | 2.342(2)      | 2.341(2)      |
| Ca2-O3d | × 2 | 2.510(2)      | 2.526(2)      | 2.557(2)      | 2.554(2)      |
| Ca2-O3e | × 2 | 2.349(1)      | 2.344(2)      | 2.352(2)      | 2.355(1)      |
| Mean    |     | 2.464         | 2.466         | 2.480         | 2.479         |
| Ca2-O4  |     | 2.391(1)      | 2.411(1)      | 2.4089(6)     | 2.413*        |
| P-O1    |     | 1.530(2)      | 1.537(2)      | 1.525(2)      | 1.526(2)      |
| P-O2    |     | 1.533(2)      | 1.529(2)      | 1.513(2)      | 1.512(2)      |
| P-O3    | × 2 | 1.526(2)      | 1.527(2)      | 1.521(2)      | 1.521(2)      |
| Mean    |     | 1.529         | 1.530         | 1.520         | 1.520         |

Notes: a = 1 - x, 1 - y, -z; b = 1 - y, x - y, z; c = 1 - x + y, 1 - x, z; d = 1 + x, y, z; e = 1 + x - y, x, -z.

\* O4 (of type A2 carbonate and OH<sup>-</sup> ions) not on c axis, resulting in three values for Ca2-O4 in the average structure, varying from 2.276 to 2.484 Å.

**TABLE 3.** Experimental details for X-ray structural analysis

| Experiment                                            | PC17    | PC16    | PC18         | PC18       |
|-------------------------------------------------------|---------|---------|--------------|------------|
|                                                       |         |         | nujol stored | dry stored |
| Crystal                                               | xt372   | xt374   | xt371        | xt373      |
| Crystal size ( $\text{mm}^3 \times 10^3$ )            | 0.13    | 0.23    | 0.49         | 0.21       |
| Crystal shape                                         | prism   | prism   | cube         | tablet     |
| Formula weight                                        | 1003.8  | 1008.3  | 1017.5       | 1019.8     |
| $D_x$ ( $\text{g}/\text{cm}^3$ )                      | 3.150   | 3.148   | 3.153        | 3.159      |
| Reflections – unique                                  | 561     | 565     | 569          | 570        |
| - number, with ( $I < 3\sigma(I)$ )                   | 264     | 277     | 308          | 252        |
| - $R_{\text{int}}^*$                                  | 0.034   | 0.035   | 0.029        | 0.027      |
| Refined parameters                                    | 44      | 43      | 57           | 56         |
| $\mu^*$ ( $\text{cm}^{-1}$ )                          | 29.2    | 29.2    | 28.7         | 28.6       |
| $R^\dagger$                                           | 0.025   | 0.025   | 0.025        | 0.025      |
| $R_w^\dagger$                                         | 0.023   | 0.024   | 0.021        | 0.022      |
| $s^\dagger$                                           | 1.25    | 1.35    | 1.19         | 1.35       |
| Extinction ( $\times 10^4$ )                          | 1.04(7) | 0.26(6) | 0.51(6)      | 0.29(6)    |
| $\Delta\rho^\ddagger$ ( $\text{e}/\text{\AA}^3$ ) (+) | 0.60    | 0.58    | 0.50         | 0.47       |
| (-)                                                   | 0.37    | 0.42    | 0.39         | 0.47       |

\*  $R_{\text{int}}$  is residual index for intensities of equivalent reflections;  $\mu$  is linear absorption coefficient.

† Least-squares refinement parameters:  $R$  is residual index;  $R_w$  is weighted residual index;  $s$  is goodness-of-fit.

‡  $\Delta$  is residual electron density.

**TABLE 4.** Atomic coordinates and isotropic displacement parameters ( $\text{\AA}^2$ )

| Site occupancy |          | $U_{eq} = (1/3) \sum_i \sum_j U^{ij} a^i a^j \mathbf{a}_i \cdot \mathbf{a}_j$ |            |           | $U, U_{eq}$ |
|----------------|----------|-------------------------------------------------------------------------------|------------|-----------|-------------|
|                |          | $x$                                                                           | $y$        | $z$       |             |
| xt372 (PC17)   |          |                                                                               |            |           |             |
| Ca1            | 1.0      | 2/3                                                                           | 1/3        | 0.0017(1) | 0.0148(5)   |
| Ca2            | 1.0      | 0.99304(8)                                                                    | 0.24700(8) | 1/4       | 0.0137(2)   |
| P              | 0.976(3) | 0.3688(1)                                                                     | 0.3988(1)  | 1/4       | 0.0101(3)   |
| O1             | 1.0      | 0.4845(2)                                                                     | 0.3289(2)  | 1/4       | 0.0150(5)   |
| O2             | 1.0      | 0.4649(2)                                                                     | 0.5866(2)  | 1/4       | 0.0200(6)   |
| O3             | 0.988    | 0.2580(2)                                                                     | 0.3432(2)  | 0.0714(2) | 0.0240(4)   |
| O4             | 0.5      | 0                                                                             | 0          | 0.1950(7) | 0.023(2)    |
| H              | 0.72(5)  | 0                                                                             | 0          | 0.053*    | 0.023*      |
| OB3            | 0.014(3) | 0.36*                                                                         | 0.43*      | 0.47*     | 0.025*      |
| xt374 (PC16)   |          |                                                                               |            |           |             |
| Ca1            | 1.0      | 2/3                                                                           | 1/3        | 0.0018(1) | 0.0156(5)   |
| Ca2            | 1.0      | 0.99268(8)                                                                    | 0.24830(9) | 1/4       | 0.0158(2)   |
| P              | 1.0      | 0.3689(1)                                                                     | 0.3993(1)  | 1/4       | 0.0130(3)   |
| O1             | 1.0      | 0.4845(2)                                                                     | 0.3287(2)  | 1/4       | 0.0151(5)   |
| O2             | 1.0      | 0.4649(3)                                                                     | 0.5862(2)  | 1/4       | 0.0234(7)   |
| O3             | 1.0      | 0.2587(2)                                                                     | 0.3435(2)  | 0.0710(2) | 0.0285(5)   |
| O4             | 0.5      | 0                                                                             | 0          | 0.1949(8) | 0.035(3)    |
| H              | 0.65(6)  | 0                                                                             | 0          | 0.53*     | 0.035*      |
| C              | 0.01*    | 0                                                                             | 0          | 0         | 0.025*      |
| OA12           | 0.012(3) | 0.944*                                                                        | 0.126*     | 0.527*    | 0.025*      |

## Limitations of X-ray diffraction:

Because of their extensive overlap and very weak electron density contributions, it was not possible to refine simultaneously both occupancy and displacement parameters for atoms of the carbonate ions.

(Elements with low atomic numbers, such as C, are difficult to locate precisely within the unit cell...)

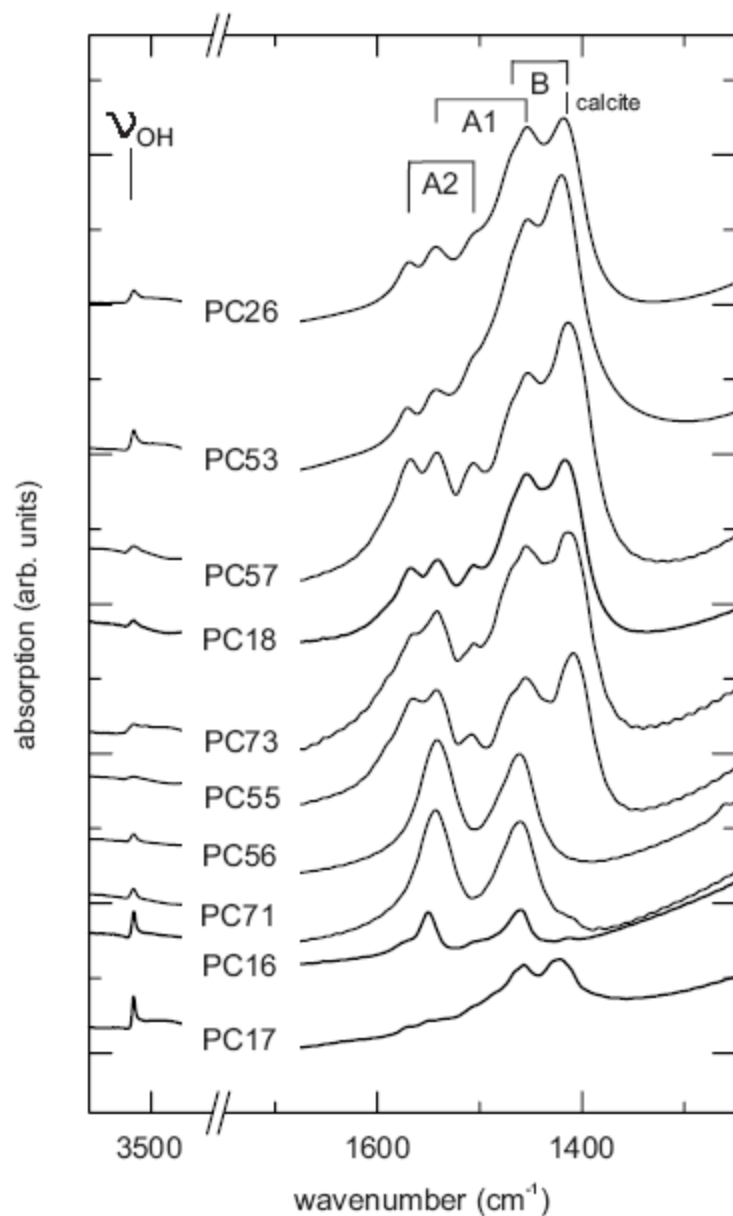
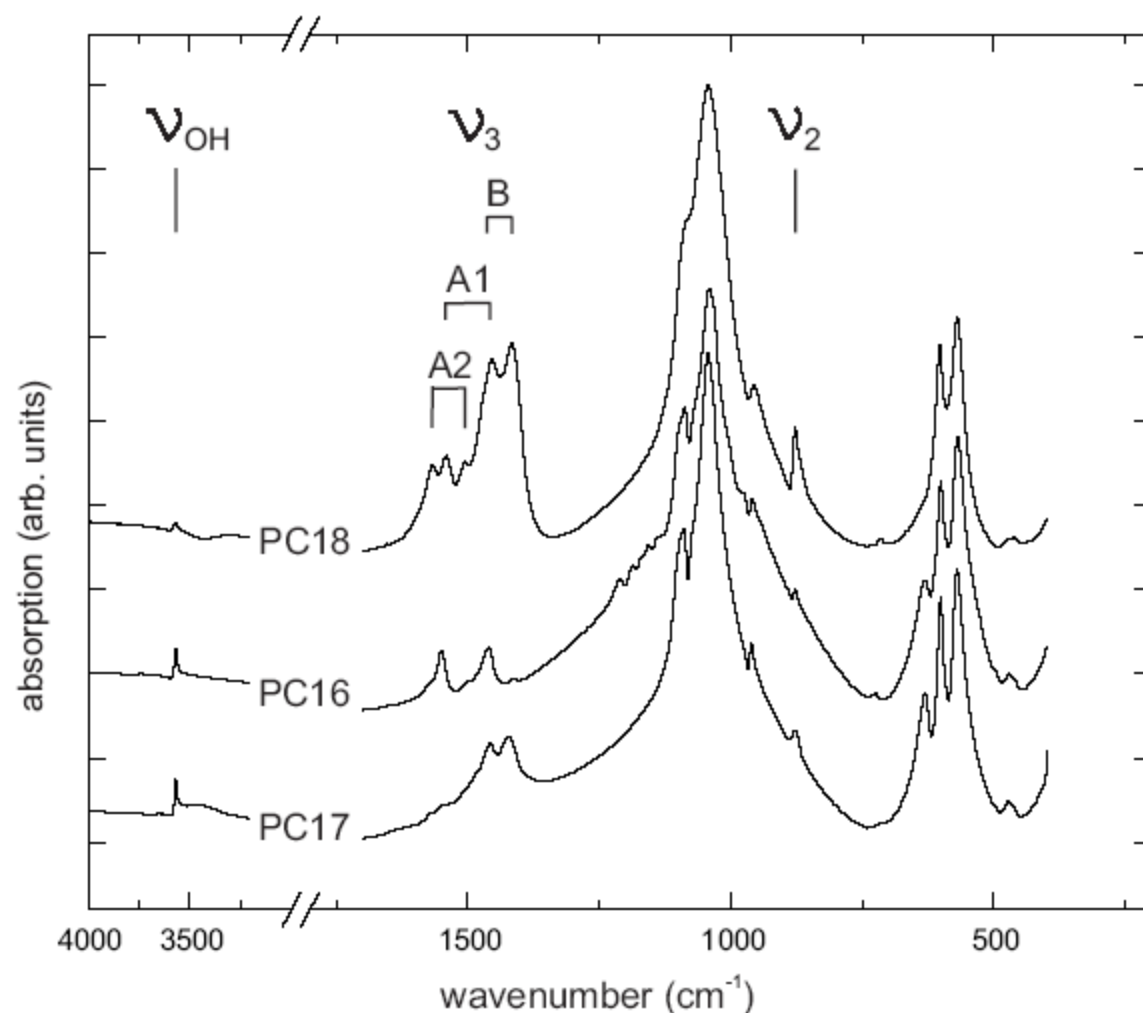


FIGURE 2. FTIR spectra of products of piston-cylinder experiments:

The C-O bond has characteristic vibration modes that can be identified by Fourier Transform Infra-Red spectroscopy.

The C-O bond does not have the same environment in the different types of substitutions. Could you show this using the GEOMETRY file?



**FIGURE 3.** FTIR spectra for synthesis experiments yielding apatites investigated by X-ray structural analysis in this study, identifying bands due to OH stretching ( $\nu_{\text{OH}}$ ) and asymmetric stretching ( $\nu_3$ ) and out-of-plane bending ( $\nu_2$ ) of carbonate ion: PC17 is type B C-OHAp; PC16 is type A C-OHAp; and PC18 is type A-B CAp; note the relatively high content of OH in PC17 and PC16 (see Table 2 footnote).



In summary, the FTIR spectra (Figs. 2–5) may be used to infer information on  $\text{OH}^-$  and  $\text{CO}_3^{2-}$  in the experimental products, in the following manner:

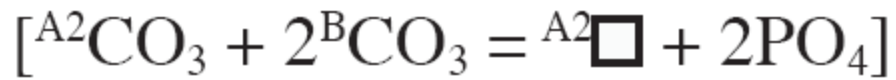
- (1) the area of the sharp band at  $\sim 3570 \text{ cm}^{-1}$  is proportional to the content of  $\text{OH}^-$  in the apatite channel, with PC71 containing about  $0.25 (\text{OH})_2$  per formula unit (pfu);
- (2) calcite is characterized by a singlet carbonate asymmetric stretching band at  $\sim 1410 \text{ cm}^{-1}$ ;
- (3) type B carbonate is characterized by the doublet of the high-frequency shoulder to the  $\sim 1455 \text{ cm}^{-1}$  band and the band at  $\sim 1410 \text{ cm}^{-1}$ ;
- (4) type A1 carbonate is characterized by the doublet of bands at  $\sim 1540$  and  $\sim 1455 \text{ cm}^{-1}$ ;
- (5) type A2 carbonate is characterized by the doublet of bands at  $\sim 1565$  and  $\sim 1505 \text{ cm}^{-1}$ .

However, the entry of moderate amounts of carbonate ion into the stuffed A2 channel location does appear to be a high-pressure feature.

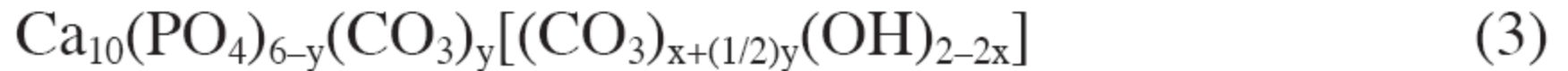
Bands attributable to type A2 carbonate are only weakly present in IR spectra of low-pressure CAp, as a sharp peak or shoulder at  $\sim 1500\text{ cm}^{-1}$  and diffuse absorption at higher frequency (Nelson and Featherstone 1982; Vignoles et al. 1988; Barralet et al. 1998; Suetsugu et al. 1998).

Therefore, charge compensation for carbonate-for-phosphate substitution in low-pressure CAp is different from that in high-pressure CAp.

Description of substitution scheme in high-pressure carbonate-hydroxylapatite:



And a formula for high-pressure CAp:



Likely, the incorporation of carbonate ions in low-temperature, biogenic hydroxylapatite involves nonstoichiometry in the Ca positions, as well as partial substitution of Ca by Na, in bone and enamel.

Can you suggest a substitution scheme (written as an equation) involving the  $\text{OH}^-$  and  $\text{CO}_3^{2-}$  groups, as well as  $\text{Ca}^{2+}$  and  $\text{Na}^+$  ?

Would your suggestion(s) result in non-stoichiometry in the Ca positions?

If this is the formula for a high-pressure carbonate-hydroxylapatite...



How would we write the formula for the low-pressure carbonate-hydroxylapatite?